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COURSE PROGRAMME

1. Information about the programme

1.1 University	University "Alexandru Ioan Cuza" of Iaşi
1.2 Faculty	Faculty of Mathematics
1.3 Department	Mathematics
1.4 Domain	Mathematics
1.5 Cycle	Master
1.6 Programme / Qualification	Applied Mathematics

2. Information about the course

2.1 Course Name			Scientific calculus				
2.2 Course taught	by		Associate Professor PhD Ionel-Dumitrel Ghiba				
2.3 Seminary / labo	orato	ry taught by	Associate Professor PhD Ionel-Dumitrel Ghiba				
2.4 Year 2 2.5 Semester			3	2.6 Type of evaluation	Ε	2.7 Course type	OP
* OB – Obligatory / OP – Optionally / F – Facultative							

OP – Optionally Iga itory

3. Total Hours (estimated per semester and activities)

3.1 Number of hours per week	4	3.2	course	2	3.3. seminary/laboratory	2
3.4 Total number of hours	56	3.5	course	28	3.6. seminary/laboratory	28
Distribution						
Individual study using textbooks, course	e notes	s, biblio	graphy item	s, etc.		60
Supplimentary study (library, on-line pla	atforms	s, etc.)				30
Individual s tudy for seminary/laboratory, homeworks, projects, etc.					25	
Tutoring						
Examination						4
Other activities						
3.7 Total hours of individual activity						119
3.8 Total hours per semester						175
3.9 Credit points						7

4. Pre-requisites

4.1 Curriculum	Mathematical Analysis, Linear Algebra
4.2 Competencies	Operation with basic notions of mathematical analysis and linear algebra. Basic knowledge of Computer Programming would be helpful.

5. Conditions (if necessary)

5.1 Course	Laboratory room (computers with MATLAB installed) Webex (if necessary)
5.2 Seminary / Laboratory	Laboratory room (computers with MATLAB installed) Webex (if necessary)



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6. Specific competencies acquired

Professional competencies	C1 Manipulating notions, methods and mathematical models, specific techniques in scientific calculus and applications C2 Being able to construct and apply mathematical methods for analyzing and simulating some processes C3 Being able to develop, analyze and test algorithms and specific programming languages; being able to use them for solving problems in applied mathematics
Transversal	CT1 Having a responsible attitude towards scientific research and teaching, being able to fully develop the personal potential in the professional career, respecting the principles of a rigorous and efficient work in order to fulfill complex tasks, respecting the ethical norms and principles in the professional activity.
competencies	CT2 Being able to make a selection of information resources and to use them efficiently, in Romanian or other language of international circulation.

7. Course objectives

7.1. General obiective	Using knowledge gained from previous courses taken (linear algebra, mathematical analysis, numerical analysis, optimization) in order to find and/or approximate the solutions of certain real problems, to obtain numerical algorithms, and to implement them in Matlab. Being able to generalize the results, when practice will demand.				
7.2. Specific ohiectives	 If successfull at the final examination, students will be able to: Explain the basic methods used during the semester. Describe the analitical methods of solving the studied problems. Use the studied numerical algorithms and the basic optimization tehniques. Analyze the solutions of the specific studied problems. Use Matlab as a calculus tool. 				

8. Contents

8.1	Course	Teaching methods	Remarks (number oh hours, references)
1.	Short presentation of the topics. Evaluation details. Global and Local Optima for Unconstrained Optimization, Clasification of Matrices. Matrix norms. Second Order Optimality Conditions, Quadratic Functions	Questioning, dialogue, lecture, proof	4
2.	Least Squares: "Solution" of Overdeterminated Systems, Data Fitting. Regularized Least Squares and applications (Denoising and Circle Fitting)	Questioning, dialogue, lecture, proof	3
3.	Descent Directions Methods. The Gradient Method	dialogue, lecture, proof	2
4.	The Condition Number for Quadratic Minimization Problem, Diagonal Scaling	Questioning, dialogue, lecture, proof	2



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_		Questioning,				
5.	Convergence Analysis of the Gradient Method	dialogue,	2			
		lecture, proof				
		Questioning,				
6.	The Gauss—Newton Method, Fermat-Weber Problem	dialogue,	3			
		lecture, proof				
	Pure Newton's Method, Damped Newton's Method, The	Questioning,				
7.	Cholesky Factorization, Hybrid Gradient-Newton Method	dialogue,	4			
	Cholesky Factorization, Hybrid Gradient-Newton Method	lecture, proof				
	Linear Programming with Matlab: The Setup, Formulating	Questioning				
8.	the Problem and a Graphical Solution. Linear Algebra-A	Questioning,	4			
о.	Constructive Approach: Jordan Exchange, Linear	dialogue,	4			
	Independenc; Vertices and extreme points;	lecture, proof				
	The Simplex Method: Example and discussion, the	Questioning				
0	Phases of the algorithm, Finite Termination; Linear	Questioning,	4			
9.	Programs in Nonstandard Form-Transforming Constraints	dialogue,	4			
	and Variables	lecture, proof				
Biblic	ography		·			
	references:					
	W. Gander, M.J. Gander, F. Kwok. Scientific computing-A	An introduction using N	Maple and MATLAB.			
	Vol. 11. Springer Science & Business, 2014.		1			
2.		ear programming with	MATLAR Vol 7			
۷.	SIAM, 2007.					
2		Algorithms and A 1	instigna with			
3.	Amir Beck, Introduction to nonlinear optimization-Theory,	, Algorithms, and Appl	ications with			
	MATLAB, SIAM, 2014.					
4.	Other references:					
		Teaching	Remarks			
8.2	Seminary / Laboratory	Teaching methods	(number oh hours,			
8.2		methods				
8.2	Short presentation of the topics. Evaluation details.	methods Questioning,	(number oh hours,			
	Short presentation of the topics. Evaluation details. Global and Local Optima for Unconstrained Optimization,	methods	(number oh hours, references)			
8.2	Short presentation of the topics. Evaluation details. Global and Local Optima for Unconstrained Optimization, Clasification of Matrices. Matrix Norms. Second Order	methods Questioning,	(number oh hours,			
	Short presentation of the topics. Evaluation details. Global and Local Optima for Unconstrained Optimization,	methods Questioning,	(number oh hours, references)			
	Short presentation of the topics. Evaluation details. Global and Local Optima for Unconstrained Optimization, Clasification of Matrices. Matrix Norms. Second Order Optimality Conditions, Quadratic Functions	methods Questioning, dialogue, exercises	(number oh hours, references)			
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	Short presentation of the topics. Evaluation details. Global and Local Optima for Unconstrained Optimization, Clasification of Matrices. Matrix Norms. Second Order Optimality Conditions, Quadratic Functions Least Squares: "Solution" of Overdeterminated Systems, Data Fitting. Regularized Least Squares and applications	methods Questioning, dialogue, exercises	(number oh hours, references)			
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1. 2. 3.	Short presentation of the topics. Evaluation details. Global and Local Optima for Unconstrained Optimization, Clasification of Matrices. Matrix Norms. Second Order Optimality Conditions, Quadratic Functions Least Squares: "Solution" of Overdeterminated Systems, Data Fitting. Regularized Least Squares and applications (Denoising and Circle Fitting) Descent Directions Methods. The Gradient Method	methodsQuestioning, dialogue, exercisesQuestioning, dialogue, exercisesQuestioning, duestioning,	(number oh hours, references) 4 3 2			
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9.	The Simplex Method: Example and discussion, the Phases of the algorithm, Finite Termination; Linear Programs in Nonstandard Form-Transforming Constraints and Variables	Questioning, dialogue, exercises	4			
Main	references:					
1.	1. W. Gander, M.J. Gander, F. Kwok. Scientific computing-An introduction using Maple and MATLAB.					
	Vol. 11. Springer Science & Business, 2014.					
2.	2. M. Ferris, C. Michael, O. L. Mangasarian, S.J. Wright. Linear programming with MATLAB. Vol. 7.					
	SIAM, 2007.					
3	Amir Beck Introduction to nonlinear optimization-Theory Algorithms and Applications with					

3. Amir Beck, Introduction to nonlinear optimization-Theory, Algorithms, and Applications with MATLAB, SIAM, 2014.

9. Coordination of the contents with the expectations of the community representatives, professional associations and relevant employers in the corresponding domain

The aim of Scientific Calculus is to give students the oportunity to understand how they may use previously acquired theoretical knowledge in order to obtain solutions of some practical problems using some algorithms and some well known mathematical software.

10. Assessment and examination

Activity	10.1 Criteria	10.2 Modes	10.3 Weight in the final grade (%)			
10.4 Course	Knowledge and correct use of fundamental concepts, results and algorithms	Written examination (WE) N1 Oral examination (OE) N2	75			
10.5 Seminary/ Laboratory	Application of analytical and numerical methods for solving some optimization problems	Evaluation during the semester N3	25			
10.6 Minimal requirements						
- Knowledge of the fundamental notions, understanding the main results						
- Development of algorithms for solving a problem of low-difficulty grade						
Final mark=(3*(N1+N2)/2+N3)/4>4.5						

Date Course coordinator 01.10.2023 Associate Professor Ionel-Dumitrel Ghiba

Seminary coordinator Associate Professor Ionel-Dumitrel Ghiba

Aproval date in the department

Head of the departament Prof. PhD. Ioan Bucataru